

Lecture 3

How to minimize cost

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Acknowledgement

- Andrew Ng's ML class
 - <https://class.coursera.org/ml-003/lecture>
 - <http://www.holehouse.org/mlclass/> (note)
- Convolutional Neural Networks for Visual Recognition.
 - <http://cs231n.github.io/>
- Tensorflow
 - <https://www.tensorflow.org>
 - <https://github.com/aymericdamien/TensorFlow-Examples>

Hypothesis and Cost

$$H(x) = Wx + b$$

$$\text{cost}(W, b) = \frac{1}{m} \sum_{i=1}^m (H(x^{(i)}) - y^{(i)})^2$$

Simplified hypothesis

$$H(x) = Wx$$

$$\text{cost}(W) = \frac{1}{m} \sum_{i=1}^m (Wx^{(i)} - y^{(i)})^2$$

What $cost(W)$ looks like?

$$cost(W) = \frac{1}{m} \sum_{i=1}^m (W x^{(i)} - y^{(i)})^2$$

x	Y
1	1
2	2
3	3

- $W=I, cost(W)=?$

What $cost(W)$ looks like?

$$cost(W) = \frac{1}{m} \sum_{i=1}^m (W x^{(i)} - y^{(i)})^2$$

x	Y
1	1
2	2
3	3

- $W=1, cost(W)=0$

$$\frac{1}{3}((1 * 1 - 1)^2 + (1 * 2 - 2)^2 + (1 * 3 - 3)^2)$$

- $W=0, cost(W)=4.67$

$$\frac{1}{3}((0 * 1 - 1)^2 + (0 * 2 - 2)^2 + (0 * 3 - 3)^2)$$

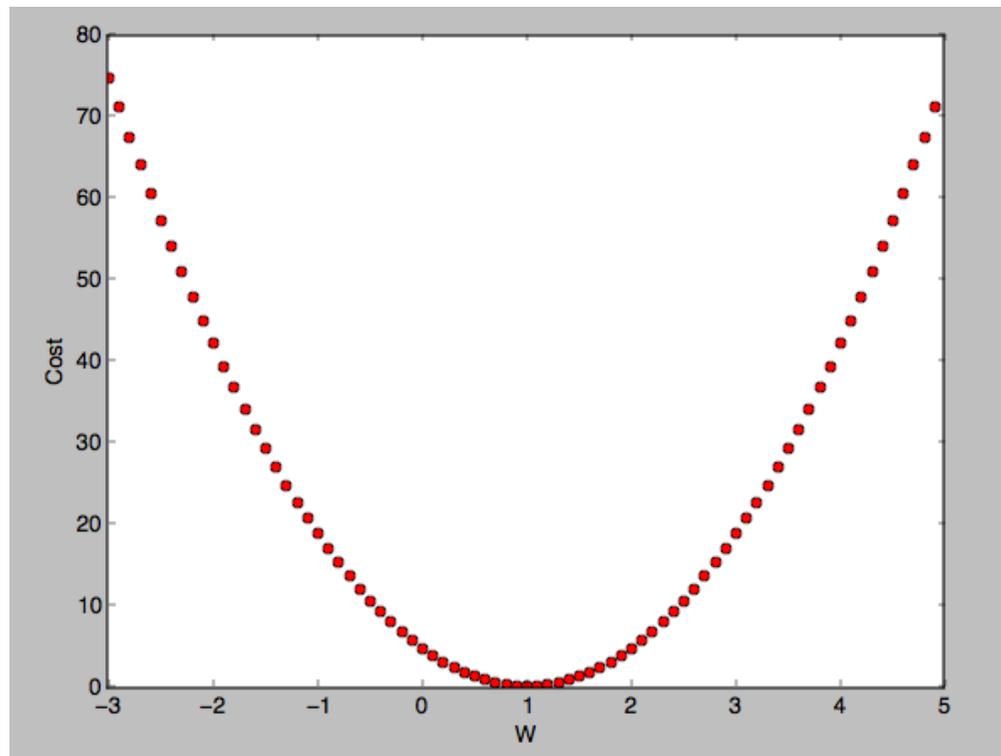
- $W=2, cost(W)=?$

What $\text{cost}(W)$ looks like?

- $W=1, \text{cost}(W)=0$
- $W=0, \text{cost}(W)=4.67$
- $W=2, \text{cost}(W)=4.67$

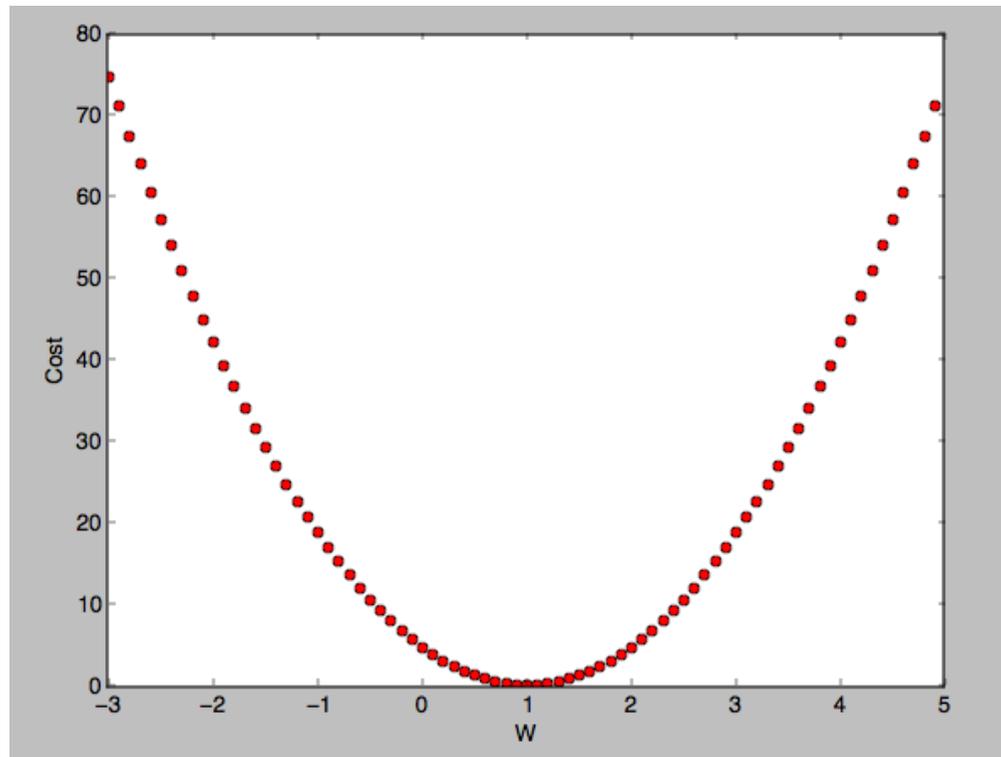
What $cost(W)$ looks like?

$$cost(W) = \frac{1}{m} \sum_{i=1}^m (W x^{(i)} - y^{(i)})^2$$



How to minimize cost?

$$\text{cost}(W) = \frac{1}{m} \sum_{i=1}^m (W x^{(i)} - y^{(i)})^2$$

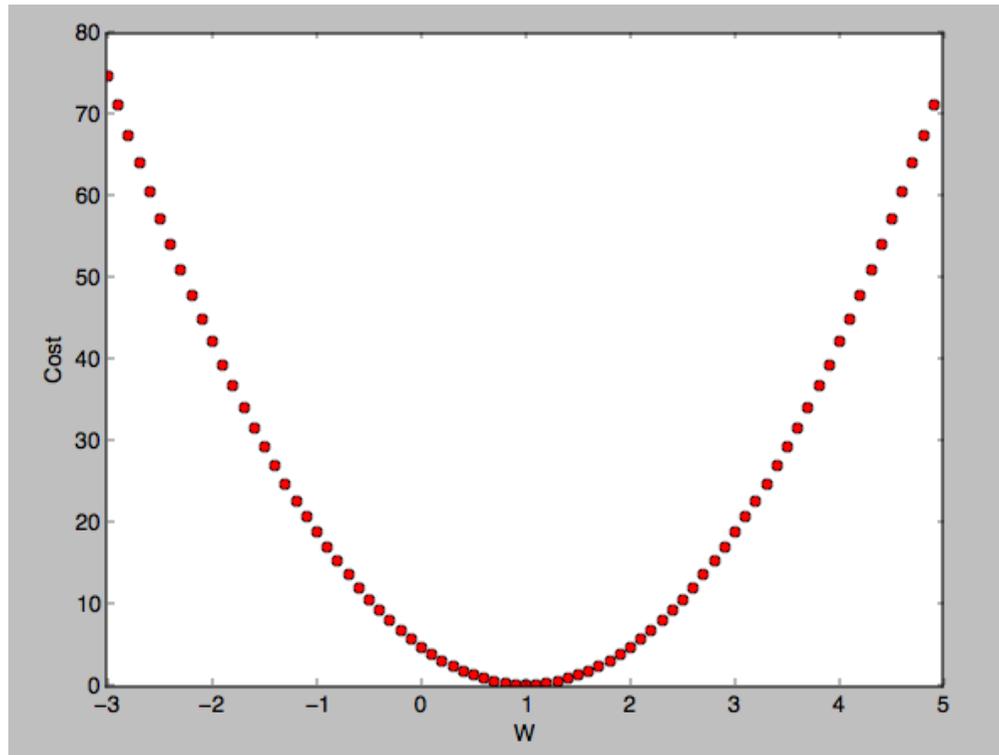


Gradient descent algorithm

- Minimize cost function
- Gradient descent is used many minimization problems
- For a given cost function, $cost(W, b)$, it will find W, b to minimize cost
- It can be applied to more general function: $cost(w_1, w_2, \dots)$

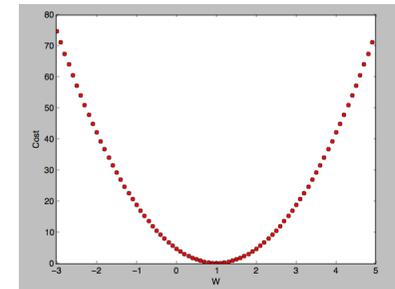
How it works?

How would you find the lowest point?



How it works?

- Start with initial guesses
 - Start at 0,0 (or any other value)
 - Keeping changing W and b a little bit to try and reduce $\text{cost}(W, b)$
- Each time you change the parameters, you select the gradient which reduces $\text{cost}(W, b)$ the most possible
- Repeat
- Do so until you converge to a local minimum
- Has an interesting property
 - Where you start can determine which minimum you end up



Formal definition

$$\text{cost}(W) = \frac{1}{m} \sum_{i=1}^m (W x^{(i)} - y^{(i)})^2$$



$$\text{cost}(W) = \frac{1}{2m} \sum_{i=1}^m (W x^{(i)} - y^{(i)})^2$$

Formal definition

$$\text{cost}(W) = \frac{1}{2m} \sum_{i=1}^m (Wx^{(i)} - y^{(i)})^2$$

$$W := W - \alpha \frac{\partial}{\partial W} \text{cost}(W)$$

Formal definition

$$W := W - \alpha \frac{\partial}{\partial W} \frac{1}{2m} \sum_{i=1}^m (W x^{(i)} - y^{(i)})^2$$

$$W := W - \alpha \frac{1}{2m} \sum_{i=1}^m 2(W x^{(i)} - y^{(i)}) x^{(i)}$$

$$W := W - \alpha \frac{1}{m} \sum_{i=1}^m (W x^{(i)} - y^{(i)}) x^{(i)}$$



Derivative Calculator

Calculate derivatives online
— with steps and graphing!

Also check the [Integral Calculator!](#)
Ableitungsrechner auf Deutsch



Calculate the Derivative of ...

Go!

This will be calculated:

$$\frac{d}{dx} \left[(xa - y)^2 \right]$$

Not what you mean? *Use parentheses!* Set differentiation variable and order in "Options".

[About](#) [Help](#) [Examples](#) [Options](#)

The Derivative Calculator lets you calculate derivatives of functions online — for free!

Our calculator allows you to check your solutions to calculus exercises. It helps you practice by showing you the full working (step by step differentiation).

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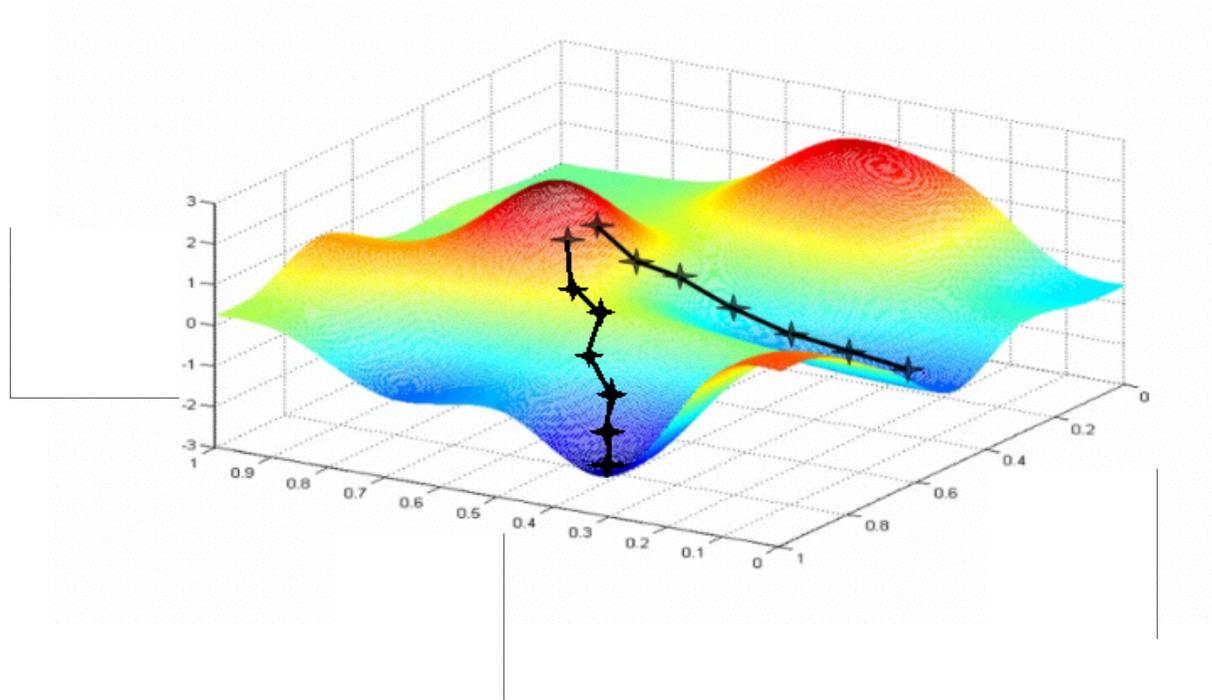
Result

Done! See the result further below.

Gradient descent algorithm

$$W := W - \alpha \frac{1}{m} \sum_{i=1}^m (W x^{(i)} - y^{(i)}) x^{(i)}$$

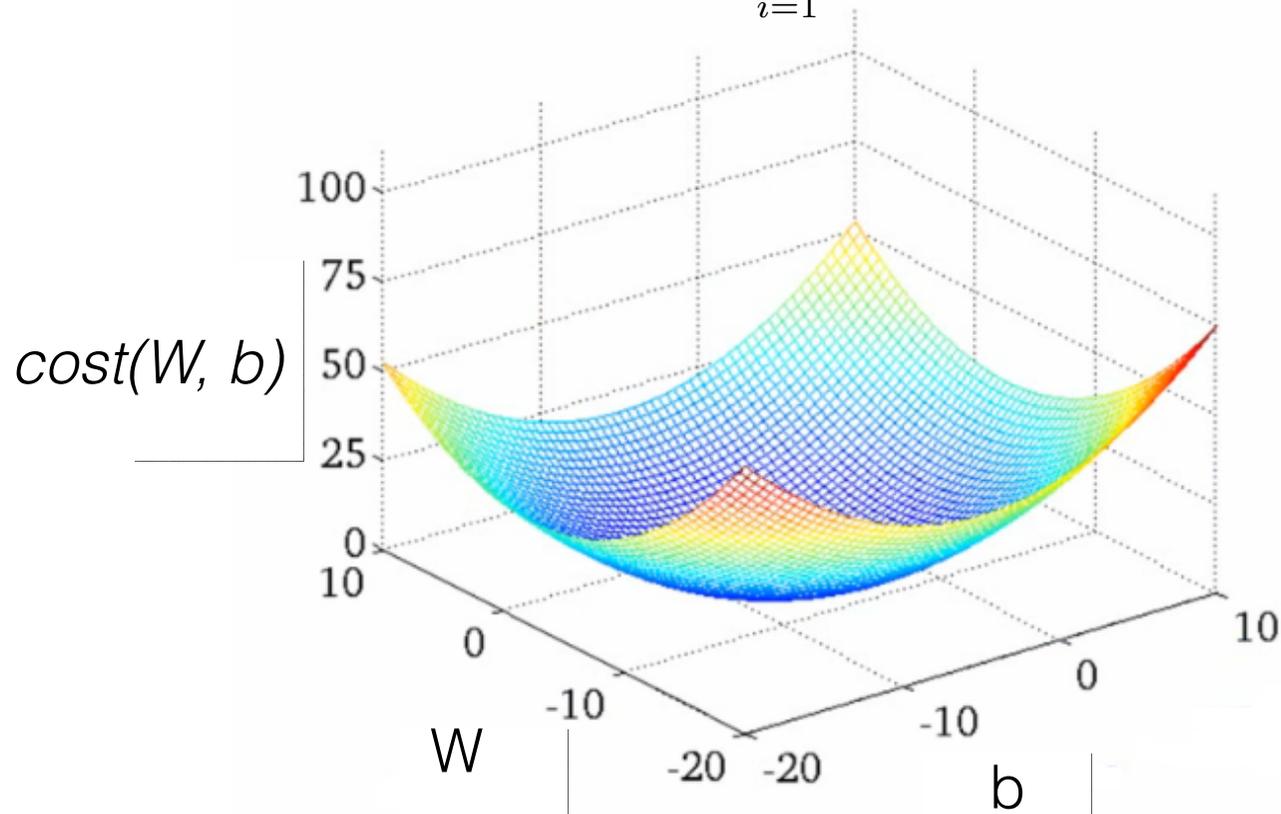
Convex function



www.holehouse.org/mlclass/

Convex function

$$\text{cost}(W, b) = \frac{1}{m} \sum_{i=1}^m (H(x^{(i)}) - y^{(i)})^2$$



Next
Multivariable logistic
regression

